

1 **MODELING STOPPING SIGHT DISTANCE**  
2 **ON LEFT-TURN CURVES OF FREEWAYS**  
3 **OVERLAPPED WITH CREST VERTICAL CURVES**

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**1 ABSTRACT**

2 This paper investigates potential Stopping Sight Distance (SSD) violation for 130km/h vehicle  
3 speed, on the passing lane of left curved, divided highways overlapped with crest vertical curves.

4 The authors previously developed a SSD control methodology that relates concurrently  
5 the 3D configuration of a roadway to the dynamics of a vehicle moving along the actual roadway  
6 path, which is applied for the assessment of critical design parameters directly related to both  
7 demanded and available SSD values.

8 Initially, by utilizing control geometric and driver - obstacle values adopted by AASHTO  
9 2011 design policy, excessive SSD inadequacy areas were revealed. Subsequently, on the basis  
10 of a classic statistical and explanatory modeling approach for a number of geometry parameters,  
11 an evaluation of SSD sufficiency was carried out in terms of both the probability of SSD  
12 inadequacy and the prediction of the object height in order to grant SSD adequacy (amended  
13 object height). These models may be useful to researchers and practitioners aiming to evaluate  
14 the interaction of the utilized design parameters in terms of the presence and the extent of SSD  
15 deficiency.

16 The results suggested that the probability modelling approach was efficient, yielding a  
17 model which enables to correctly assess SSD adequacy (by more than 94%) in such 3D road  
18 alignments. The lognormal modelling approach for the prediction of the amended object height  
19 (AOH) was proved somewhat less accurate when the AOH exceeds 1 metre, and further analysis  
20 is required in order to fully investigate the non-linear relationships between the examined  
21 variables and the amended object height.

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## 1 INTRODUCTION AND PROBLEM STATEMENT

2 In current highway design practice (e.g. 1-4), the three-dimensional highway geometry is still  
3 addressed by designing it in two independent and mostly uncorrelated two-phase, two-  
4 dimensional stages, namely, the horizontal alignment and the vertical profile. This 2-D approach,  
5 while inevitable in many cases, has proven to be associated with design misconceptions that  
6 influence the design performance adversely. Such a typical case of design misconception is the  
7 determination of the critical parameter of Stopping Sight Distance (SSD).

8 The 2-D SSD calculation is inexact, fragmentary and may produce design deficiencies  
9 due to inaccurate calculation of the available sight distance. Hassan et al. (5), for example, stated  
10 that 2-D SSD investigation might underestimate or overestimate the available sight distance and  
11 consequently lead to design criteria violation. Furthermore, a pure 2-D SSD design control can  
12 be detrimental to the cost or performance of a divided highway, since in case of SSD inadequacy  
13 a usual solution is either an increase of the inner shoulder width or to a decrease of the posted  
14 speed under wet pavement conditions, the latter being a common case in Europe due to a lack of  
15 available land. Therefore, contemporary highway design policies try to define 3-D design rules  
16 that assist designers efficiently and address the SSD inadequacy problem. For example, the  
17 Green Book (1) stresses that, in order SSD provision to be granted, the vertical curve should be  
18 entirely designed inside the horizontal curve. In the Spanish Design Guidelines (4) the desired  
19 horizontal – vertical curve arrangement is reached when the vertical crest curve falls completely  
20 inside the horizontal curve, including spirals. However, such provisions do not actually address  
21 all design cases and, therefore, a final 3-D perspective evaluation of the roadway  
22 is inevitable (2).

23 One of the first researchers that assessed the available sight distance on 3-D alignment,  
24 Sanchez (6), studied the interaction between the sight distance and the 3-D combined alignment  
25 idealized into a net of triangles using Inroads software. Although this methodology was accurate,  
26 it was very time consuming since the available sight distance was determined graphically (not  
27 analytically).

28 Several years later, Hassan et al. (7) presented an analytical model for computing  
29 available sight distance on combined horizontal and vertical highway alignments using  
30 parametric finite elements (4, 6 and 8-node rectangular elements, as well as 3-node triangular  
31 elements) to represent the highway and sight obstructions. The proposed model examined the  
32 driver's sight line, which was represented by a straight line between the driver's eye and an  
33 object, against all the possible sight obstructions by using an iterative procedure.

34 Lovell et al. (8) developed a method to calculate the sight distance based on horizontal  
35 geometry, without considering the effect of vertical geometry. Nehate and Rys (9) described a  
36 methodology to define the available sight distance using Global Positioning System (GPS) data  
37 by examining the intersection of line of sight with the elements representing the road surface.  
38 However, the available sight distance was not based on the road's compound (horizontal and  
39 vertical) alignment.

40 In the past years, in order to evaluate the actual sight distance in real driving conditions, a  
41 number of 3-D models are found in the literature (10-16) aiming to optimize the available sight  
42 distance.

43 Recently, Kim and Lovell (17) delivered a 3-D sight distance evaluation method where  
44 an algorithm is used to determine the maximum available sight distance using computational  
45 geometry and thin plate spline interpolation to represent the surface of the road. The available  
46 sight distance is measured by finding the shortest line that does not intersect any obstacle.

1 Jha et al. (18) proposed a 3-D methodology similar to the present paper for measuring  
 2 sight distance, utilizing triangulation methods via an algorithm consisting of three stages- road  
 3 surface development, virtual field of view surface development, and virtual line of sight plane  
 4 development .The process involved multiple software platforms, thus delivering an accurate but  
 5 non-flexible outcome.

6 As already stated above, most of the previously mentioned research studies are focused in  
 7 optimizing the available SSD by introducing either new algorithms or design parameter  
 8 combinations, ignoring in many cases the topographic visual restraints. Moreover, none of the  
 9 above mentioned approaches suggested a comprehensive methodology to simulate from a 3-D  
 10 perspective concurrently both the alignment design and the vehicle dynamics on the road surface  
 11 during emergency braking.

### 12 **SSD MODELING PROPOSAL**

13 The SSD adequacy investigation that follows is an accurate procedure, based on a realistic  
 14 representation of the roadway features as well as the vehicle dynamics. The process is based on  
 15 the difference between the available and the demanded SSD, where SSD adequacy is granted  
 16 when:  
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$$18 \text{SSD}_{\text{DEMANDED}} \leq \text{SSD}_{\text{AVAILABLE}} \quad (1)$$

19  
 20 On one hand,  $\text{SSD}_{\text{DEMANDED}}$  is defined based on the point mass model introduced by  
 21 many design guidelines worldwide, enriched by the actual values of grade and friction variation  
 22 due to the effect of vertical curves and vehicle cornering respectively. It is worth noting that in  
 23 such alignments, the above actual grade and friction values are ignored in current practice.  
 24 Therefore, by utilizing an iteration process through the laws of mechanics, the vehicle's speed  
 25 reduction was determined based on the actual tire-road friction interaction.  $\text{SSD}_{\text{AVAILABLE}}$ , on the  
 26 other hand, is termed as the driver's line of sight towards the object height, both at a certain  
 27 offset in 3D roadway environment. Equations of analytical geometry are utilized in order to  
 28 describe the above mentioned line of sight and determine its intersection points with planes  
 29 formed by the road geometry or features that restrict the driver's vision towards the object.

30 The developed procedure, analytically outlined through 19 and 20, among others  
 31 identifies areas of interrupted vision lines between driver and object at left-turn curves due to the  
 32 presence of median concrete barriers.  
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34 Consequently, through the suggested approach, the authors aim initially in defining areas  
 35 where the overlaid crest vertical curvature on horizontal curved alignments generates SSD  
 36 inadequacies. Such an effort was partially addressed through a recent work of the authors (21),  
 37 where, for the design speed of 130km/h and for a wide range of horizontal and vertical design  
 38 values, certain arrangements of such compound alignments were precluded in terms of SSD  
 39 inadequacy. However, this assessment was confined from the utilization of a single value  
 40 referring to inner shoulder width. Therefore, in the present paper a range referring to the most  
 41 typical inner shoulder width values is utilized as well in order to develop statistical models  
 42 capable of:

- 43 • Estimating the probability of SSD inadequacy
- 44 • Predicting the additional object height in order to grant SSD adequacy (referred in
- 45 the present paper as amended object height)

## 1 **MEDIAN BARRIER DESIGN ON DIVIDED HIGHWAYS**

2 Roadside barriers are placed in the longitudinal direction of high-speed roadways to redirect  
3 errant vehicles and shield them from hitting obstacles along either side of the road (1, 22). The  
4 presence of median barriers on left-turn curved, divided highways, although increasing the level  
5 of safety, under certain circumstances may affect the sight distance available to drivers (23).

6 The selection process of the appropriate traffic barrier type is a complicated task since  
7 many parameters are involved, where the most important goals to be served are safety,  
8 operational and economic considerations. As for providing SSD adequacy, the barrier height, and  
9 especially the clearance between the barrier and the left edge of the passing lane, known as inner  
10 shoulder width (ISW), seems to be the most critical issues (e.g. 1, 24).

11 Since on divided highways, in cases of potential vehicle collisions, rather shallow impact  
12 angles are expected, at least in the median areas, as well as for maintenance reasons, rigid  
13 concrete barrier types seem to be more appropriate (22). However, in any utilized median barrier  
14 type, vehicles travelling on the opposite direction should not interrupt the driver's line of sight.  
15 Figure 1a and 1b shows a cross-section example of "New Jersey" concrete barrier type with  
16 0.81m height, as shown in Roadside Design Guide (22).

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## 18 **EXISTING SIGHT DISTANCE APPROACH ON LEFT CURVED DIVIDED** 19 **HIGHWAYS**

20 Although the necessity for SSD adequacy on left-turn curves of divided highways is emphasized  
21 in current design practice (e.g. 1-4, 25), no explicit process is provided to accurately implement  
22 this control. The only available tool in defining the available SSD is the 2D approach according  
23 to which  $SSD_{AVAILABLE}$  is defined by the lateral clearance and the curve radius. However this  
24 consideration applies only to circular curves longer than the sight distance where both driver and  
25 obstacle are positioned on the circular curve (1). Moreover, between the driver height and the  
26 obstacle height, there is no assurance whether the barrier height and/or the presence of a vertical  
27 curve does not obstruct the driver's line of sight.

28 The breakpoint of SSD adequacy in current practice is defined by equalizing  
29  $SSD_{AVAILABLE}$  and  $SSD_{DEMANDED}$  (Equation 1) where two different options exist:

- 30 • the determination of the examined curve's inferred safe speed referring to the given  
31 geometry (horizontal, vertical, typical cross-section) which may reflect the area's posted  
32 speed value;
- 33 • the definition of the inner shoulder width for a desired speed value on the curved road  
34 geometry

35 Based on this concept, many researchers addressed their concerns in SSD provision for  
36 left-turn curved divided highways. For example, Arndt (26) mentioned that the SSD adequacy  
37 process using the design criteria listed in the current design guidelines would lead to very wide  
38 shoulders, which was described as uneconomical, where in case of maintaining the original  
39 shoulder widths, rather conservative speed limit values should be implemented (27). Therefore,  
40 the adoption of the conventional approach, given by the current practice, besides the cost or  
41 performance impacts, may lead to road safety violation as well, since either the widened inner  
42 shoulder potentially can be used as an extra traffic lane for passing maneuvers especially by  
43 motorcyclists, or areas with unexpected speed discontinuity will emerge.

44 Klam et. al. (28), aiming to improve available SSD in intersection areas, suggested the  
45 arrangement of shorter barriers (0.508m high), referred to as low-profile barriers, in different  
46 locations in Texas and Florida, where merely the Test Level 2 criteria (70km/h) of the NCHRP

1 Report 350 (29) were reached. To increase the Test Level a stabilized rail was suggested to be  
2 attached to the low-profile barrier.

3 In another research (30), the risk evaluation of inadequate available SSD due to the  
4 presence of median barriers was examined via reliability analysis. A methodology was presented  
5 to calculate the probability of non-compliance that describes the associated risk of a driver  
6 requiring a sight distance greater than available in order to make a safe stop. However, since the  
7 simple 2D approach was utilized for available sight distance, the accuracy of the results is  
8 uncertain.

9 Sarhan et. al. (23) using a previously developed software, examined the impact of  
10 roadside and median barriers on the available SSD on horizontal curves when overlapped with  
11 various vertical alignments. The results confirmed previous findings according to which the  
12 available sight distance depends on the type of the vertical alignment and the curvature of crest  
13 or sag vertical curves overlapping on the horizontal curve.

14 In AASHTO design guidelines, as far as divided highways are concerned, the  
15 recommended distance between the edge of the travelled way and the median barrier could  
16 deliver available SSD values less than the relevant required (23).

17 Although the conventional SSD approach is adopted in the German RAA 2008 design  
18 guidelines as well, in situations of SSD shortage, it is recommended to modify the road  
19 alignment or decrease the speed limit. However, in every case SSD adequacy is advised to be  
20 assessed in 3D roadway environment, where no further instructions are provided (2).

21 Since the conventional approach practically fails to address SSD adequacy, in certain  
22 cases (25), less-conservative criteria for the parameters involved in the SSD adequacy process  
23 are introduced which are believed to be more realistic (ex. increased values of deceleration rate  
24 and obstacle height).

25 As the design policies worldwide associate vehicle speed with the definition of critical  
26 vertical design parameters via SSD provisions based in 2D approach, the existence of a reliable  
27 tool to effectively and accurately perform SSD adequacy investigation on compound alignments  
28 for a given speed value seems essential.

29 Moreover, aiming to provide a clear outlook of the interaction as well as appropriate  
30 arrangement between the horizontal and vertical alignment, none of the relevant research studies  
31 examined the impact of median barriers on SSD adequacy concurrently from the 3D alignment  
32 design viewpoint along with the vehicle dynamics.

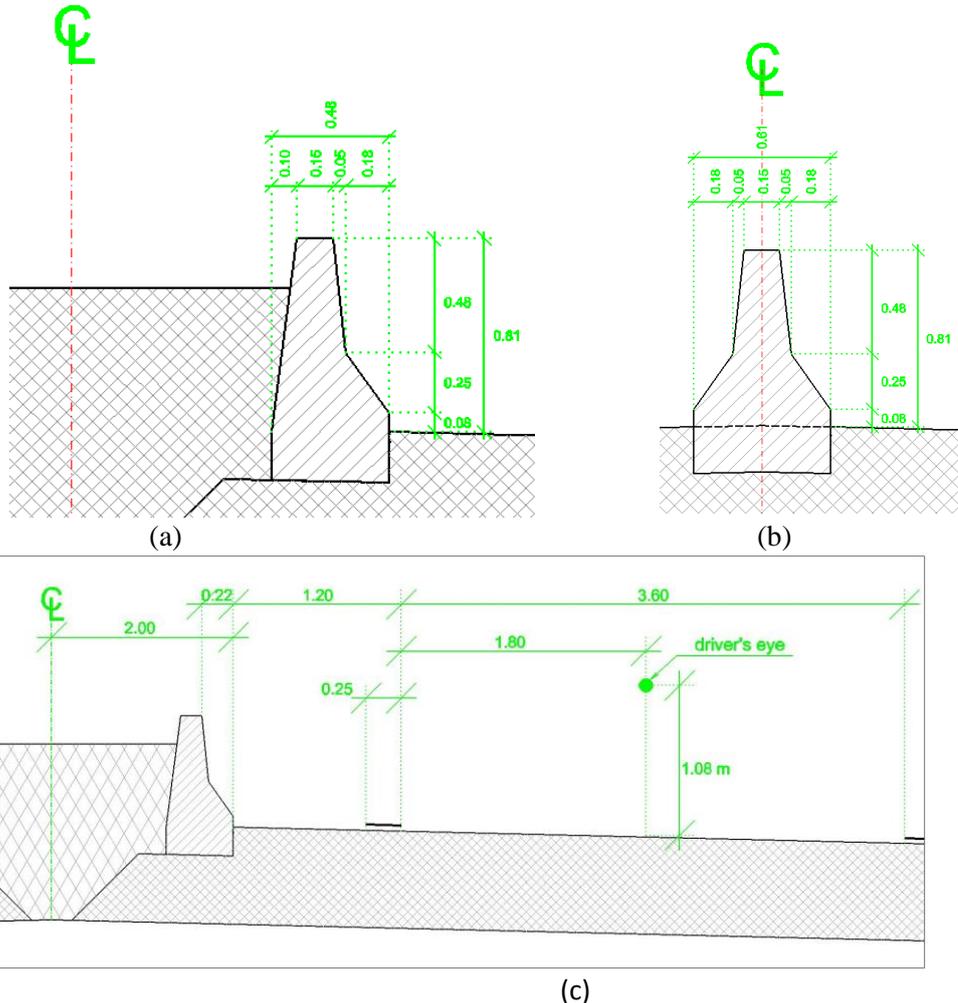
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### 34 **3D SSD ADEQUACY INVESTIGATION FOR AASHTO 2011 DESIGN POLICY ON** 35 **LEFT CURVED DIVIDED HIGHWAYS**

36 In order to investigate potential safety violation for AASHTO 2011 design guidelines, certain  
37 cases of left-turn curved, divided highway segments were examined. Initially, the utilized design  
38 parameters for the selected design speed of 130km/h represent control values [R=950m  
39 (horizontal radius) for e=6% (superelevation rate), K=125m (rate of crest vertical curve)]. It is  
40 clear that the speed value of 130km/h refers to the roadway's posted speed, of which the road  
41 surface condition is assumed wet.

42 Since, according to AASHTO 2011, the maximum grade value for 130km/h assuming  
43 rolling terrain is set to 4%, the crest vertical curve's boundary grade values were set to -4% and  
44 4% (symmetrical) respectively. As far as the ISW is concerned, based once again on AASHTO,  
45 values ranging from 1.20m – 2.40m were utilized.

1 A cross section example at the barrier area is shown through Figure 1c and consists of a  
 2 passing lane and an inner shoulder of 3.60m and 1.20m respectively (AASHTO 2011). The  
 3 median barrier of Figure 1c is a “New Jersey” type with height of 0.90m (0.81m plus safety  
 4 margin), where its curvature at the top increases the inner shoulder by 0.22m (Figure 1c).



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 8 NOTE: (a: single sided, b: double sided).

9 **FIGURE 1 Example Dimensions of “New Jersey” Concrete Median Barrier Type (a), (b)**  
 10 **and Semi Cross Section View at the Inner Shoulder Area (c).**

11  
 12 As far as the driver’s eye and object heights are concerned, 1.08m and 0.60m were  
 13 assumed (AASHTO 2011), where the deceleration rate and the driver’s perception – reaction  
 14 time were taken as  $3.40\text{m/sec}^2$  and 2.5sec respectively (AASHTO 2011). Finally, the lateral  
 15 offsets of both driver and obstacle from the edge of the passing lane (Figure 1c) were assumed  
 16 half of the lane width (1.80m).

17 As already stated, the sight line in median barriers should not be allowed in any case to  
 18 go beyond the edge of traveled way on the opposite direction so that the available SSD would  
 19 not depend on whether there is a vehicle in the opposite direction. Therefore, simple calculations  
 20 (21) revealed that by utilizing the control value of  $R=950\text{m}$ , the Median Width (MW) should be  
 21  $2 \times 4\text{m}$ , where for  $R > 1435\text{m}$ , a median width of  $2 \times 2\text{m}$  was used as shown in Figure 1c (note that  
 22  $MW \geq 2 \times 1.5\text{m}$  for AASHTO 2011).

1 An example of the driver's sightline being obstructed at the barrier area of a left-turn  
2 curved divided highway is shown in Figure 2a, where three types of SSD deficiencies can be  
3 seen - the hidden sightline by the barrier area (blue line), the (max) vertical distance below the  
4 NJ area (green line), and the amended object height (red line) in order for SSD at the examined  
5 station to be granted.

6 The SSD adequacy assessment in the present paper, was carried out by utilizing the  
7 following stages: alignment selection; definition of calculation step (100m in the present  
8 analysis) where the driver's vehicle is positioned; calculation of  $SSD_{DEMANDED}$ ;  $SSD_{AVAILABLE}$   
9 forced equal to  $SSD_{DEMANDED}$ ; calculation of intersection points between the driver to object  
10 sightline and the median barriers area in 3D; record of these points in order to calculate, for the  
11 most unfavorable case, the vertical difference of the sightline from the barriers' top as well as the  
12 amended object height in order the driver's sightline to be non-obstructed due to the median  
13 barriers.

14 The above process initially was assessed for  $ISW=1.20m$  assuming from the horizontal  
15 alignment point of view a circular arc ( $R=950m$ ), which encloses a vertical transition area  
16 ( $K=125m$ ,  $L=1000m$ ) arranged as to allow the examination of the braking procedure of the  
17 vehicle throughout the variable grade area (prior, during and after), thus including the constant  
18 grades as well (Figure 2b).

19 Figure 2b illustrates certain sets (14 sets) of horizontal bars (4 bars per set) where SSD  
20 adequacy was examined at fixed distances every 100m. The primary (bottom) horizontal axis  
21 shows the linear projection of the horizontal circular arc where the vertical transition area  
22 (St.1500 – St.2500) is illustrated as well. The vertical axis represents the same fixed locations  
23 (every 100m) of the examined alignment where the vehicle's SSD procedure is initiated. The  
24 bars in black color show various SSD values referring to the relevant station, where the lines in  
25 blue express the length of the driver's sight line blocked by the median width in 3D perspective.  
26 Both black and blue bars are measured through the horizontal alignment's centerline. For  
27 example at St.2000, which is located inside the vertical curve, the SSD is 292.0m and the sight  
28 line is blocked twice (St.2030 – St.2119 and St.2171 – St.2267). From the length of the SSD bars  
29 it can be seen that the assessment besides the areas of constant grade incorporates the effect of  
30 the vertical transition as well. The secondary (top) horizontal axis of Figure 2b quantifies the  
31 max vertical distance of the sightline below the New Jersey barrier (dashed green line) as well as  
32 the modified obstacle height (dashed red line) in order for the sightline to pass tangentially over  
33 the most unfavorable point. For the same Station (St.2000), it can be seen that somewhere inside  
34 the relevant two blue lines the sightline intersects the NJ barrier area 0.73m below the top, where  
35 in order to retrieve SSD adequacy, the obstacle height should be set to 2.25m.

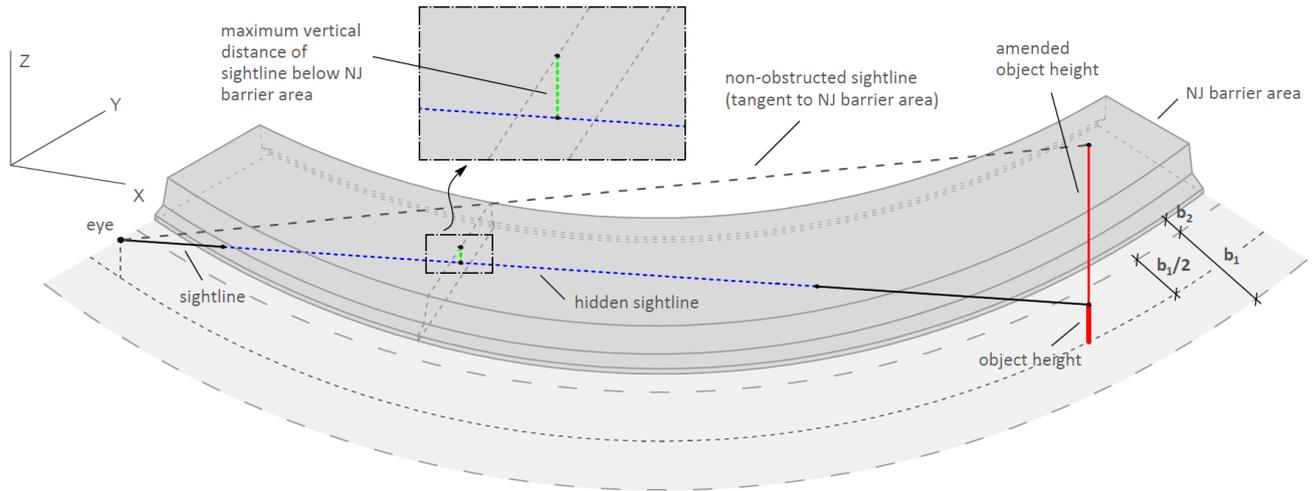
36 It is evident that the points referring to the green and red line do not necessarily coincide.  
37 The evaluation was drawn assuming 0.90m as barrier height [0.81m+safety margin (plantation,  
38 construction tolerance etc.)]. It can be seen that if the barrier height for some reason is raised by  
39 0.10m to 1.00m, the max vertical distance of the sightline below the NJ barrier area (green line)  
40 will be raised 0.10m accordingly, however not the same finding will be noticed for the new  
41 obstacle height (red line) which increases as a function of the distance from the driver's eye. As  
42 a result, assuming as barrier height the original value of 0.81m, SSD adequacy would be granted  
43 only in the constant grade area (St.1200 and St.2500 respectively).

44 In Figure 2b the most critical SSD inadequacy area is found in the negative grade area  
45 and close to the end of the vertical transition (St.2200), where the obstacle height should be  
46 raised up to 2.44m in order to be visible.

1           Commenting further on Figure 2b, it can be seen that AASHTO 2011 design guidelines  
2 fail to warrant safety during emergency braking of a vehicle moving with 130km/h on the  
3 passing lane of such a left curved divided highway geometry, since the median barrier obstructs  
4 the line sight between driver (1.08m) and object (0.60m) heights. At first glance this finding is  
5 not surprising since by applying basic geometric considerations the barrier height (0.90m) is  
6 greater than the average heights between the driver and the obstacle. Moreover, this assumption  
7 overestimates the actual available SSDs on curved horizontal sections overlapped with crest  
8 vertical curves (5).

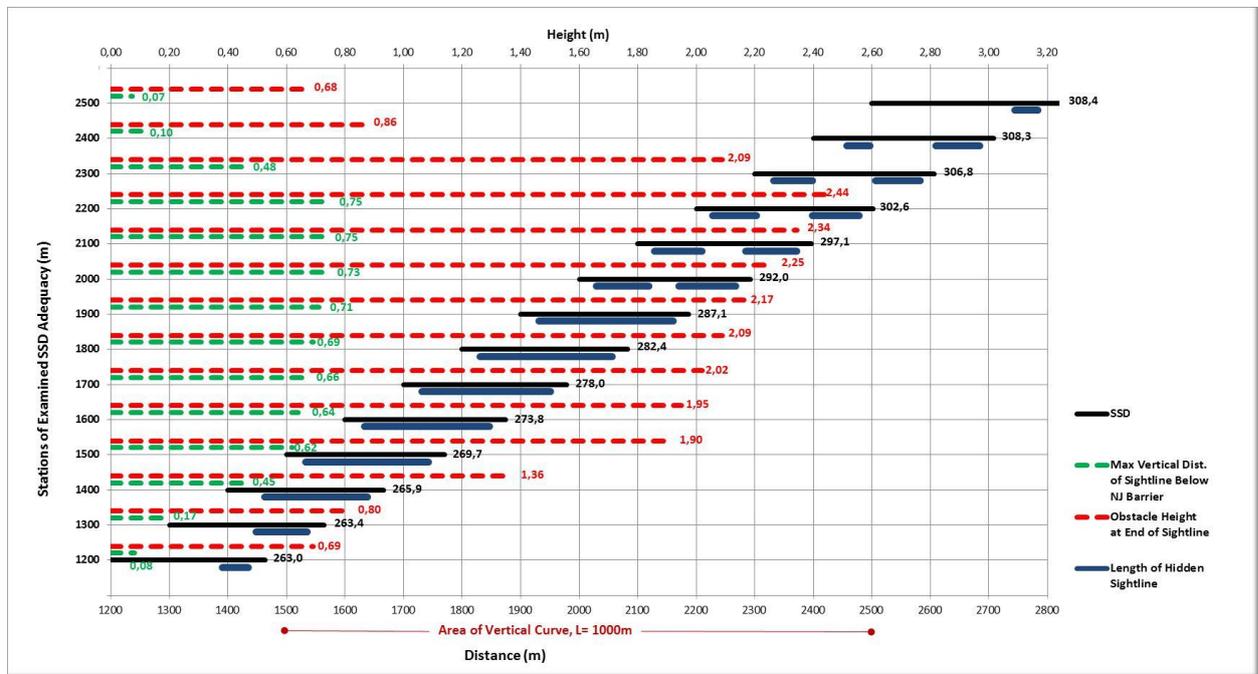
9           From the above process it can be seen that although SSD adequacy can be accurately  
10 calculated for any arrangement, the analytical model is computationally demanding. Moreover  
11 there is a clear need for practitioners to be informed in advance regarding the interaction of the  
12 utilized design parameters selection in terms of SSD adequacy.

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Note:  $b_1$ : passing lane,  $b_2$ : inner shoulder width.

(a)



(b)

**FIGURE 2 SSD Adequacy Investigation on Compound Alignment of Left Curved Divided Highway (R=950m, K=125m, ISW=1.20m, All Possible Arrangements Examined).**

**MODELS DEVELOPMENT**

In several recent studies (e.g. 30, 31) probabilistic approaches, such as simulation and reliability analysis, are proposed as an appealing option for identifying SSD inadequacy patterns. In this paper, an interpolation approach on the basis of key SSD critical situations is proposed instead to provide a simple, generic and flexible tool for the assessment of SSD adequacy. More

1 specifically, SSD is modelled in terms of evaluating the probability of SSD inadequacy and  
 2 predicting the amended object height in case of SSD deficiencies. Regarding the first case, a  
 3 logistic regression model is developed for the estimation of the probability of the required SSD  
 4 exceeding the relevant available, where an amendment of the object height is inevitable. In the  
 5 latter case, the amended object height itself (i.e. the increment of the object height over the  
 6 control value of 0.60m) is estimated on the basis of the road geometric design elements in 3D  
 7 context.

8 The main explanatory variables considered include the horizontal (R) and vertical (K)  
 9 curvatures, the grades (s1, s2) which refer to the starting and ending grade values of the braking  
 10 procedure, their difference (ds), as well as the inner shoulder width (ISW). More specifically, for  
 11 the initially selected calculation step (100m), the grade value s1 was calculated based on the  
 12 selected vertical curvature (K). The ending grade value of the braking process (s2) was  
 13 calculated as a function of the selected horizontal (R) and vertical (K) curvatures' explanatory  
 14 variables. By equalizing  $SSD_{AVAILABLE}$  to  $SSD_{DEMANDED}$  and utilizing the selected ISW value  
 15 outputs similar to Figure 2b were delivered. A number of alignment arrangements were formed  
 16 by combining the following variables:

- 17 • Horizontal radii values (950m, 1500, 2000m, 2500m, 3000m, 3500m)
- 18 • Vertical curvature rates (125m, 200m, 250m, 300m, 350m, 400m)
- 19 • ISW (1.20m, 1.80m, 2.40m)

20 In other words, for every possible arrangement of the above variables, graphs similar to  
 21 Figure 2b were extracted resulting from the performed SSD adequacy investigation in advance,  
 22 along, and beyond the vertical transition area, formed by the grade values of +4% and -4%  
 23 respectively. In total, 2772 different alignment cases were examined.

24 In order to enhance the explanatory performance of the models, selected interactions of  
 25 these variables were also tested on the basis of the insights already obtained by the  
 26 implementation of the analytical approach. Moreover, specific conditions were addressed by  
 27 means of dedicated variables in order to capture not only the core cases along the main curve  
 28 (e.g. non linear relationship between horizontal curve radius and SSD inadequacy) but also the  
 29 marginal cases at the boundaries of the curve (e.g. at the constant grade section).

30 A likelihood ratio test was used to assess model quality, and the quality of the predictions  
 31 was the ultimate criterion for selecting the optimal model.

### 33 **Logistic Regression Modelling of the Probability of SSD Inadequacy**

34 The specification of the SSD inadequacy model is given by Equation 2, with  $\pi_{ij}$  the probability  
 35 of SSD inadequacy,  $X_i$  the explanatory variables,  $\beta_i$  parameters to be estimated and  $\varepsilon_i$  the  
 36 logistically distributed  $\sim[0, \mu]$  error term, as follows:

$$38 \quad \text{Logit}(\pi_{ij}) = \text{Log}\left(\frac{\pi_{ij}}{1-\pi_{ij}}\right) = \sum \beta_i X_i + \varepsilon_i \quad (2)$$

39 In particular, the logit link function expresses the logarithm of the odds of SSD  
 40 inadequacy, i.e. the logarithm of the ratio of the probability of SSD inadequacy to the probability  
 41 of SSD adequacy. A binary logistic regression model is fitted to the data.

42 The parameter estimates, their marginal effects (Exp(B)), their elasticities and goodness-  
 43 of-fit measures of the best fitting model are presented in Table 1a. It is noted that, while marginal  
 44 effects Exp(B) express the change in the odds of SSD inadequacy for 1 unit increase of the  
 45 explanatory variable, elasticities express the related % change in the odds for 1% increase of the

1 explanatory variable; in this sense, elasticities are easier to interpret, as they are dimensionless  
 2 and unconditional to the measurement units of explanatory variables. The final model is shown  
 3 through Equation 3 as follows:

$$4 \quad \text{Logit}(\pi_{ij}) = \text{Log}\left(\frac{\pi_{ij}}{1-\pi_{ij}}\right) = 0.18*K + 0.009*R - 0.162*s1 - 11,568*D_s - 5.15*ISW -$$

$$6 \quad 0.002*R^2 - 0.008*K*D_s + 0.004*R*D_s - 0,00000705*K*R + 0.782*D_s*s1 + \varepsilon_i \quad (3)$$

7  
 8 This model can be analysed as follows: on one hand, there are variables referring to all  
 9 the examined alignments, i.e. R, s1, ISW; and on the other, there are variables and interactions  
 10 concerning alignments within a vertical curve, i.e. K, ds, K\*ds, R\*ds and s1\*ds. Obviously,  
 11 when ds equals zero, the model describes alignments on constant grade values of +4% or -4%.

12 The parameter estimates of the main effects suggest that an increase of the vertical  
 13 curvature increases the probability of SSD inadequacy. More specifically, the elasticity indicates  
 14 that a unit increase in vertical curvature rate increases the odds of SSD inadequacy by more than  
 15 3 times (3.4). On the basis of the insights from the analytical estimation, a quadratic form of the  
 16 effect of horizontal curvature was considered, and the results confirmed this specification, as the  
 17 parameters of both R<sup>2</sup> and R were statistically significant. In particular, the parameter of R is  
 18 positive (elasticity equals 1,51 i.e. 151% increase of the odds of inadequacy for each 1% increase  
 19 of R) and the parameter of R<sup>2</sup> is negative, which corresponds to a parabola, i.e. as R increases,  
 20 the probability of SSD inadequacy initially increases up to a certain point, from which the  
 21 probability of SSD deficiency decreases. These findings were also noticed from a previous  
 22 research of the authors (21).

23 On the other hand, an increase in the ISW decreases the probability of SSD inadequacy,  
 24 by 68% per 1% increase (elasticity equals -0,680). Moreover, an increase in grade at the  
 25 beginning of the braking procedure (s1) and an increased difference between the grades at the  
 26 starting and ending points of the braking procedure (ds)<sup>1</sup> decrease the probability of SSD  
 27 inadequacy by 0,8% and by 62%, per 1% increase respectively. In other words, the negative  
 28 grade area of the vertical curve is more critical in terms of SSD inadequacy due to the increase of  
 29 the demanded SSD.

30 The interactions suggest that the combined effect of vertical curvature and grade  
 31 difference decreases the probability of SSD inadequacy, while the other combined effects (i.e.  
 32 horizontal curvature and grade difference, horizontal and vertical curvature, grade at the  
 33 beginning of the braking procedure and grade difference) increase the probability of SSD  
 34 inadequacy.

35 The likelihood ratio test leads to accept the model compared to the null model, and a  
 36 pseudo R-squared (estimated as 1-LL/LL0) (32) is equal to 0.79, which is very satisfactory for  
 37 this type of model. In fact, logistic regression models may have an upper limit lower than 1  
 38 in the maximum R-squared value that can be achieved, due to the likelihood-based estimation  
 39 instead of ordinary least squares estimation, as well as to the nature of the response variable (32,  
 40 33).

41 Table 1b summarises the classification of cases on the basis of the model predictions.  
 42 More specifically, the Table presents a cross-classification of observed and predicted values for

---

<sup>1</sup> It is noted that (ds) takes negative values, and consequently the elasticities of parameters including (ds) may have different sign from the parameter estimates B, as the elasticities are calculated on the basis of the product of B (negative) with (ds) (also negative).

1 the dependent variable (i.e. probability of SSD inadequacy); for a perfectly fitting model, one  
 2 would expect the observed and predicted values to match (see highlighted parts of the table) and  
 3 the off-diagonal cells of the Table would be empty. The Table data reveal that more than 94% of  
 4 total cases are correctly classified by the model as regards SSD adequacy. The 155 cases [75+80,  
 5 (Table 1b)] of falsely classified cases - i.e. cases of observed inadequacy (value=1) which are  
 6 predicted as cases of adequacy (value=0) or vice versa - were carefully reviewed in order to  
 7 identify potential systematic failure of the model to capture particular cases. It was observed that  
 8 no systematic misclassification was identified. However, it was noticed that 51 misclassified  
 9 cases - a share of approximately 33% of the 155 misclassified cases - (i.e. about 2% of all cases)  
 10 involves alignments of constant grade (either -4% or +4%) - although, the majority of the cases  
 11 of alignments of constant grade were correctly classified by the model. It was examined whether  
 12 a more detailed specification of variables referring to the constant grade alignments (e.g. entering  
 13  $s1=-4\%$  as a distinct variable) may enhance the model but no significant improvement was  
 14 observed.

15

### 16 **Lognormal Regression Modelling of the Amended Object Height**

17 The specification of the amended object height (AOH) model was determined on the basis of a  
 18 thorough descriptive analysis of the data revealing nonlinear associations of amended object  
 19 height (i.e. the increment of the object height over the control value of 0.60m) with the examined  
 20 variables. A histogram of the response variable led to the identification of a clearly skewed  
 21 density function, suggesting a lognormal distribution (Equation 4). Consequently, with  $X_i$  the  
 22 explanatory variables,  $\beta_i$  parameters to be estimated and  $\epsilon_i$  the normally distributed  $\sim[0, \sigma^2]$  error  
 23 term, this lognormal model is formed as follows:

24

$$25 \quad \text{Log}(AOH_i) = \sum \beta_i X_i + \epsilon_i \quad (4)$$

26

27 The parameter estimates and goodness-of-fit measures of the best fitting model are  
 28 presented in Table 1c. The final model specification is as follows (Equation 5):

29

$$30 \quad \text{Log}(AOH_i) = 1.117 - 0.002 * K - 0.003 * R - 0,768 * ISW - 0.772 * D_s + 0,0000008 * K * R -$$

$$31 \quad 0.005 * K * D_s - 0,0002012 * R * D_s + ,0002100 * R * ISW - 2.499 * (s14) + 0.002 * R * (s14) + \epsilon_i \quad (5)$$

32

33 Similar to the previous case, this model can be analysed, based on variables and  
 34 interactions for all the examined alignments (i.e. R,  $s1$ , ISW,  $R * ISW$ ) or specifically for  
 35 alignments within a vertical curve (i.e. K,  $d_s$ ,  $K * d_s$ , and  $R * d_s$ ). In the latter case, a variable  
 36 specific to the case where  $s1=s2=-4\%$  ( $s14$  in Table 1c) and its interaction with the horizontal  
 37 curvature were found to be significant. Furthermore, a quadratic function of horizontal curve  
 38 radius was tested but was not found to outperform the logarithmic function with respect to  
 39 amended object height.

40

41 The parameter estimates of the main effects suggest that an increase in all main effects  
 42 (i.e. K, R, ISW,  $d_s$ ,  $s14$ ) decrease the amended object height, while all the interactions increase  
 43 the amended object height, except from  $K * d_s$  which decreases the amended object height. The  
 44 likelihood ratio test leads to accept the model compared to the null model, and a pseudo R-  
 45 squared is equal to 0.71, which is satisfactory.

46

46 A closer look at the predicted values suggest that the differences between observed and  
 predicted values are low; however, the model residuals are not white noise (i.e. unrelated to the

1 predicted values), and the plot of residuals against the predicted values suggests the presence of  
 2 a more complex non-linear relationship. In particular, an area of poor model performance was  
 3 identified with respect to cases where the observed amended object height exceeded 1m beyond  
 4 the control value of 0.60m.

7 **TABLE 1 (a) Parameter estimates and goodness-of-fit of the logistic regression model of**  
 8 **SSD inadequacy**

9 **(b) Classification of the Logistic Regression Model (observed vs. predicted SSD**  
 10 **inadequacy)**

11 **(c) Parameter Estimates and Goodness-of-Fit of the Lognormal Regression**  
 12 **Model of the Amended Object Height**

13 (a)

Parameter	B	S.E.	Wald test	p-value	Exp(B)	Elasticity
K	,01813703	,00295862	37,580	<0,001	1,018	3,404
R	,00875999	,00064639	183,663	<0,001	1,009	1,516
s1	-,16167454	,05077569	10,138	,001	,851	-0,009
Ds	-11,56791068	1,42435424	65,959	<0,001	,000	0,617
ISW	-5,15025730	,31647009	264,845	<0,001	0,006	-0,680
R <sup>2</sup>	-,00232342	,00020009	134,829	<0,001	0,998	-1,006
K * ds	-,00765764	,00269050	8,101	,004	,992	0,115
R * ds	,00375407	,00048204	60,651	<0,001	1,004	-0,513
K * R	-,00000705	,00000127	30,590	<0,001	1,000	-3,25
ds * s1	,78238421	,08736706	80,195	<0,001	2,187	-0,036
<b>Null Log-likelihood (LL0)</b>		-1864,85				
<b>Final Log-likelihood (LL)</b>		-392,825				
<b>Likelihood Ratio test</b>		2944,05				
<b>df</b>		10				
<b>pseudo R-squared</b>		0,79				

15 (b)

SSD inadequacy		Predicted		% Correct
		0	1	
Observed	0	1032	75	93,2
	1	80	1585	95,2
Total				94,4

17  
 18  
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1

(c)

Parameter	B	Std. Error	Wald Chi-Square	p-value
(Intercept)	1,1172864	,2487440	20,175	<0,001
K	-,0024194	,0003363	51,754	<0,001
R	-,0029807	,0001715	301,972	<0,001
ISW	-,7683734	,0546478	197,697	<0,001
Ds	-,7717293	,0748511	106,300	<0,001
Kx R	,0000008	,0000002	23,110	<0,001
K * ds	-,0053688	,0002712	391,984	<0,001
R * ds	-,0002012	,0000362	30,832	<0,001
R * ISW	,0002100	,0000310	45,802	<0,001
[s14=,00] * R	-2,4985374	,2694198	153,768	<0,001
[s14=1,00] * R	0		.	.
[s14=,00]	,0022574	,0001820	86,003	<0,001
[s14=1,00]	0		.	.
(Scale)	,1259748 <sup>b</sup>	,0043661		
<b>Null Log-likelihood</b>		-2198,8		
<b>Final Log-likelihood</b>		-637,8		
<b>Likelihood Ratio test</b>		3122		
<b>df</b>		10		
<b>pseudo R-squared</b>		0,71		

2

3

It is clear that the final model specification may not address all possible combinations of design parameters with the same accuracy and the logarithmic model is certainly an approximation. However, even with this imperfect specification, the model can be useful within a preliminary assessment of the design parameters as regards SSD adequacy.

6

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## CONCLUSIONS

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The research is focused in examining potential safety violations for AASHTO 2011 design guidelines, regarding SSD provision for 130km/h vehicle speed, on the passing lane of left-turn curved, divided highways overlapped with crest vertical curves for various horizontal and vertical and inner shoulder width design values.

11

12

Initially, SSD adequacy investigation was addressed through analytical calculations for control horizontal and vertical design values, where extensive SSD shortage zones were revealed inside the area of the horizontal radius.

14

15

Subsequently, an evaluation of SSD sufficiency was carried out in terms of both the probability of SSD inadequacy and the prediction of the amended object height.

17

18

The proposed statistical modelling approach may have a twofold interest. Firstly, although SSD adequacy can be accurately calculated for any arrangement, the analytical model is computationally demanding and there is a need for an efficient and applicable tool. Secondly, emphasis is given not only on the identification of the effects of road design elements on SSD adequacy, but also on the quantification of these effects (i.e. elasticities), which consists a very useful tool for practitioners. For example, a researcher or practitioner may test his or her design parameters by implementing the logistic regression model equation, and obtain the probability of SSD adequacy and the related classification of this set of design parameters (i.e. adequacy or

21

22

23

24

25

1 not). In case inadequacy is predicted, the researcher or practitioner may further implement the  
2 lognormal regression model to obtain a prediction of the AOH, which allows for some insight  
3 whether the set of design parameters needs small adjustment (e.g. small AOH) or significant  
4 adjustment (e.g. large AOH), and therefore reassess the utilized design parameters accordingly.

5 Nevertheless, the proposed explanatory approach is not without limitations, due to the  
6 complex yet deterministic nature of the relationships examined, inducing an obvious risk of  
7 overfitting the statistical models and thus yielding measurement errors in the effects identified.  
8 The challenge of the proposed approach was to develop models able to efficiently capture the  
9 key determinants of SSD adequacy and estimate SSD adequacy at a high accuracy level, so that  
10 the models may be useful to researchers and practitioners dealing with road design assessment.  
11 In that sense, model parsimony was not a priority, to the extent to which model quality and  
12 performance are not compromised.

13 The results suggest that the probability modelling approach was efficient, yielding a  
14 model which enables researchers to correctly classify SSD adequacy in such 3D road alignments.  
15 The logarithmic modelling approach of the AOH prediction is somewhat less accurate, and  
16 further analysis is required in order to fully investigate the non-linear relationships between the  
17 examined variables and the AOH. In this framework, non parametric and machine learning  
18 methods (e.g. neural networks) may be proved efficient in capturing these complex and non-  
19 linear relationships.

20 Further analysis should also aim at the cross-validation of the models, particularly as  
21 regards the unfavorable conditions, through the use of separate training and testing datasets.

22 Finally, additional work is necessary in order to examine more speed values, but mostly  
23 optimize in terms of SSD provision, the influence of additional parameters involved. Such  
24 parameters comprise the median barrier type for certain cases (e.g. bridge or tunnel areas,  
25 interchange ramps etc.), issues associated to human factors, more realistic deceleration values, as  
26 well as night time driving conditions where a more clear view of the safety margins will emerge.

## 27 REFERENCES

- 28 1. American Association of State Highway and Transportation Officials (AASHTO). *A Policy*  
29 *on Geometric Design of Highways and Streets*, Fifth Edition. Washington, DC., 2011
- 30 2. Ed.German Road and Transportation Research Association, Committee, Geometric Design  
31 Standards. *Guidelines for the Design of Roads*, (RAA), Germany, 2008.
- 32 3. Ministry of Environment, Regional Planning and Public Works. *Guidelines for the Design of*  
33 *Road Projects, Part 3, Alignment (OMOE-X)*, Greece, 2001.
- 34 4. Ministerio de Fomento. *Instrucción de Carreteras, Norma 3.1 – IC “Trazado”*, Spain, 2000.
- 35 5. Hassan, Y., Easa, S.M. and Abd El Halim A.O. Design Considerations for Combined  
36 Highway alignments. *Journal of Transportation Engineering*, Vol 123, No.1, pp. 60-68,  
37 1997.
- 38 6. Sanchez, E. Three-Dimensional Analysis of Sight Distance on Interchange Connectors. In  
39 *Transportation Research Record 1445*, TRB, National Research Council, Washington, D.C.,  
40 pp. 101–108, 1994.
- 41 7. Hassan, Y., Easa, S. M. and Abd El Halim, A.O. Analytical Model for Sight Distance  
42 Analysis on Three-Dimensional Highway Alignments, *Transportation Research Record*,  
43 Vol. 1523, 1996.
- 44 8. Lovell, D.J., Jong, J.C., and Chang, P.C. Improvement to the Sight Distance Algorithm,  
45 *Journal of Transportation Engineering*, 127(4), 283-288, 2001.
- 46

- 1 9. Nehate, G. and Rys M. 3-D calculation of stopping-sight distance from GPS data, *Journal of*  
2 *Transportation Engineering*, 132(6), Sep 2006, pp. 691-698, 2006.
- 3 10. García, A. Optimal Vertical Alignment Analysis for Highway design – Discussion. *Journal*  
4 *of Transportation Engineering*, Vol. 130, Issue 1, pp. 138, 2004.
- 5 11. Zimmermann, M. Increased Safety Resulting from Quantitative Evaluation of Sight  
6 Distances and Visibility Conditions of Two-Lane Rural Roads. *Proceedings of the 3<sup>rd</sup>*  
7 *International Symposium on Highway Geometric Design*, TRB, Chicago, USA, 2005.
- 8 12. Ismail, K. and Sayed T. New algorithm for calculating 3-D available sight distance. *Journal*  
9 *of Transportation Engineering*, Vol. 133, No.10, pp. 572-581, 2007.
- 10 13. Romero, M.A. and García A. Optimal Overlapping of Horizontal and Vertical Curves  
11 Maximizing Sight Distance by Genetic Algorithms. *The 86<sup>th</sup> Annual Meeting of the*  
12 *Transportation Research Board*, Washington, DC., 2007.
- 13 14. Yan, X., Radwan, E., Zhang, F. and Parker J.C. Evaluation of Dynamic Passing Sight  
14 Distance Problem Using a Finite - Element Model. *Journal of Transportation Engineering*,  
15 Vol. 134, No.6, pp. 225-235, 2008.
- 16 15. DiVito, M. and Cantisani G. D.I.T.S.: A Software for Sight Distance Verification and  
17 Optical Defectiveness Recognition. *Proceedings of the 4<sup>th</sup> International Symposium on*  
18 *Highway Geometric Design*, TRB, Valencia, Spain., 2010.
- 19 16. Moreno Chou, A., Perez, V., Garcia, A. and Rojas M. Evaluation of 3-D Coordination to  
20 Maximize the Available Stopping Sight Distance in Two – Lane Roads. Paper published on  
21 *The Baltic Journal of Road and Bridge Engineering*, Vol. IX, No2, 2014.
- 22 17. Kim, D. and Lovell D. A Procedure for 3-D Sight Distance Evaluation Using Thin Plate  
23 Splines. *The 90<sup>th</sup> Annual Meeting of the Transportation Research Board*, Washington, DC.,  
24 2011.
- 25 18. Jha, M., Kumar Karri, G.A. and Kuhn W. A New 3-Dimensional Highway Design  
26 Methodology for Sight Distance Measurement. *The 90<sup>th</sup> Annual Meeting of the*  
27 *Transportation Research Board*, Washington, DC., 2011.
- 28 19. Mertzanis F., A. Boutsakis, I. Kaparakis, S. Mavromatis, and B. Psarianos. *Analytical*  
29 *Method for Three-Dimensional Stopping Sight Distance*. Paper presented on the 3<sup>rd</sup>  
30 *International Conference on Road Safety and Simulation*, RSS2013, Rome, Italy, 2013.
- 31 20. Mavromatis S., Palaskas S. and Psarianos B. Continuous Three-Dimensional Stopping Sight  
32 Distance Control on Crest Vertical Curves. Paper published on *the Advances in*  
33 *Transportation Studies (ATS)*, XXVIII issue, November 2012.
- 34 21. Mavromatis S., Psarianos B., Mertzanis F. And Vardaki S. Three-Dimensional Stopping  
35 Sight Distance Control on Left-Turn Curves of Freeways Overlapped With Crest Vertical  
36 Curves. Paper presented at the 5<sup>th</sup> *International Symposium on Highway Geometric Design*,  
37 TRB, Vancouver, Canada 2015.
- 38 22. American Association of State Highway and Transportation Officials (AASHTO). *Roadside*  
39 *Design Guide*, Third Edition., Washington, D.C., 2006.
- 40 23. Sarhan, M. and Y. Hassan. Consideration of Sight Distance in Placement of Concrete  
41 Barriers on Horizontal Curves of Roads. Paper published on *TRR, 2301, TRB, National*  
42 *Research Council*, Washington, D.C., 2012.
- 43 24. Donnell, E. and J. Mason. Predicting the Frequency of Median Barrier Crashes on  
44 Pennsylvania Interstate Highways. *Accident Analysis and Prevention Journal*, Vol. 38, Issue  
45 3, 2006.
- 46 25. Austroads. *Guide to Road Design Series*. Austroads, Australia, 2009.

- 1 26. Arndt, O., R. Cox, S. Lennie and M. Whitehead. Provision of Sight Distance Around  
2 Concrete Barriers and Structures on Freeways and Interchanges. *Proceedings of the 4<sup>th</sup>*  
3 *International Symposium on Highway Geometric Design*, TRB, Spain, 2010.
- 4 27. Mavromatis, S., B. Psarianos and E. Kasapi. Computational Determination of Passenger  
5 Cars' Braking Distances Equipped with Anti-Block Brake Systems. *Proceedings of the 3<sup>rd</sup>*  
6 *International Symposium on Highway Geometric Design*, TRB, Chicago, 2005.
- 7 28. Klam, Jeremy W. and Don L. Ivery. Low-Profile Barrier with Tl-3 Modification. *Presented*  
8 *at 89th Annual Meeting of the Transportation Research Board*, Washington, D.C., 2010.
- 9 29. Ross, H.E. Jr., D.L. Sicking, R.A. Zimmer, and J.D. Michie. *Recommended Procedures for*  
10 *the Safety Performance Evaluation of Highway Features*. NCHRP Report 350,  
11 Transportation Research Board, National Research Council, Washington DC, 1993.
- 12 30. Richl, L. and T. Sayed. Evaluating the Safety Risk of Narrow Medians using Reliability  
13 Analysis. *Journal of Transportation Engineering*, Vol. 132(5), 2006, pp.366-375.
- 14 31. De Santos-Berbel C. and Castro M. Stopping Sight Distance Simulation Using a New  
15 Probabilistic Approach. Paper presented at the 5<sup>th</sup> *International Symposium on Highway*  
16 *Geometric Design*, TRB, Vancouver, Canada 2015.
- 17 32. McFadden, D. Conditional logit analysis of qualitative choice behavior. Pp. 105-142 in P.  
18 Zarembka (ed.), *Frontiers in Econometrics*. Academic Press, 1974.
- 19 33. Nagelkerke, N.J.D. A note on a general definition of the coefficient of determination.  
20 *Biometrika* 78, 1991, pp. 691-692.