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Hybrid Data Envelopment Analysis for Large-Scale Smartphone Data Modeling

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Scope

- **Methodological approach** for driving safety efficiency **benchmarking**
 - on a trip basis
 - optimization techniques
- **Smartphone** devices
 - large-scale data
 - naturalistic driving conditions
- Estimation time is **exponentially increased**
 - as more driving data are aggregated
 - improve the existing approach



Background (1/2)

- **Linear programming** for efficiency measurement
 - **Data Envelopment Analysis (DEA)**
 - Banks, Companies, Hospitals, Staff etc.
 - Transport (Systems, Traffic safety etc.)
 - Driving behaviour research
- Driving **behaviour characteristics**
 - Speeding
 - Harsh braking/ acceleration/ cornering
 - Seatbelt use
 - Mobile phone use



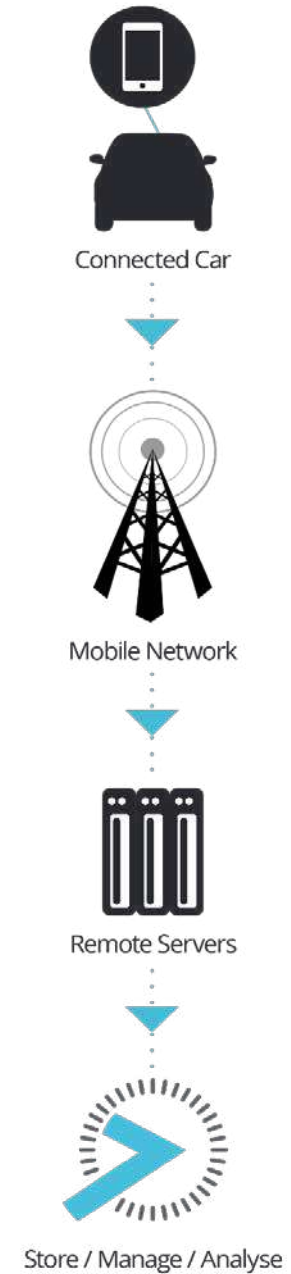
Background (2/2)

- **Data collection** schemes
 - Smartphones
 - In-vehicle devices
 - On-board diagnostic devices (e.g. OBD-II)
- **Data sources**
 - Naturalistic driving experiments
 - Driving simulator experiments
 - In-depth accident investigation



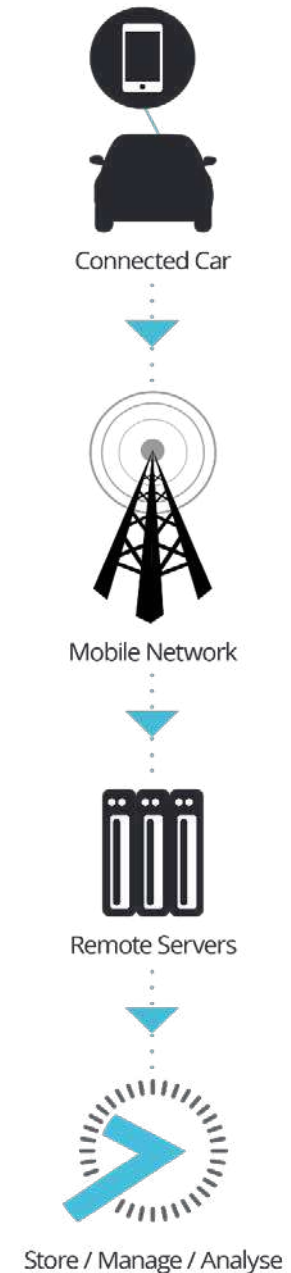
Smartphone data collection (1/2)

- A **mobile application** to record user's driving behaviour (automatic start / stop)
- A variety of **APIs** is used to read mobile phone **sensor data**
- Data is transmitted from the mobile App to the **central database**
- Data are stored in a **sophisticated database** where they are managed and processed



Smartphone data collection (2/2)

- **Indicators** are designed using:
 - machine learning algorithms
 - big data mining techniques
- Data collected for **10,088** trips from **88** drivers (From July to December 2016)
- The database analyzed was in .csv format
 - Drivers' trips are stored per row, the characteristics of which are stored in each column's variables



Data envelopment analysis (1/2)

- **Optimization technique**
 - Performance measurement using DEA
 - Companies, banks, hospitals, staff etc.
- Significant **computation cost**
 - Exact solution
 - Reduced Basis Entry (RBE)
 - Convex Hull (CH)
 - Reduce processing time
- Decision-Making-Unit (**DMU**)
 - Factory, company etc.
 - Trips, drivers
 - variables are continuous and quantitative
 - a driver should reduce the frequency of his driving characteristics for a given mileage



Data envelopment analysis (2/2)

- **Efficiency index** Driving_efficiency_B
- **Input-oriented** DEA
 - minimize inputs (number of HA, HB events etc.) per driving distance
- Constant-returns-to-scale (**CRS**) problem
 - the sum of all inputs changes proportionally to the sum of driving output (distance)
- **Efficient level** of driving characteristics for a trip/ driver
 - inputs
 - outputs

$$\min(\text{Driving_Efficiency}_B)$$

Subject to the following constraints:

$$\text{Driving_Efficiency}_B * x_o - X * \lambda \geq 0$$

$$Y * \lambda \geq y_o$$

$$\lambda_i \geq 0 \forall \lambda_i \in \lambda$$

$$Metric_i = \sum_{j=1}^m \lambda_j * Metric_j$$

$$dis\ tan\ ce_{urban} = dis\ tan\ ce_i / \text{Driving_Efficiency}_i$$



Efficiency index parameters

Risk exposure indicators:

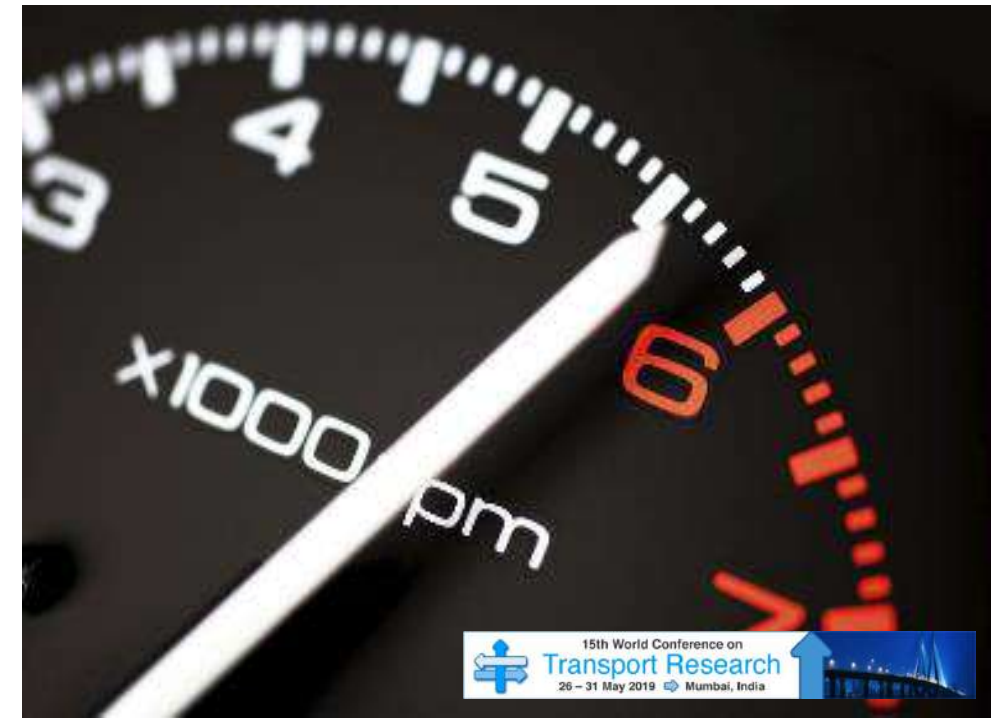
- Total **distance** travelled

Driving behaviour indicators:

- **Harsh events**
 - Number of harsh braking (longitudinal acceleration) (HA)
 - Number of harsh acceleration (longitudinal acceleration) (HB)
- **Speeding** (SP)
 - seconds driving over the speed limit
- **Mobile phone** use distraction (MU)
 - seconds using the mobile phone

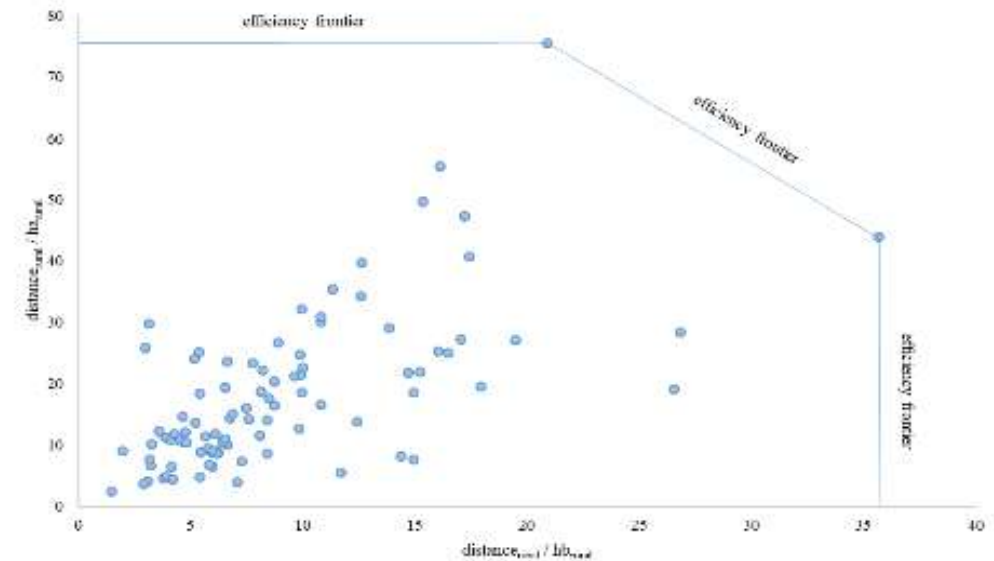
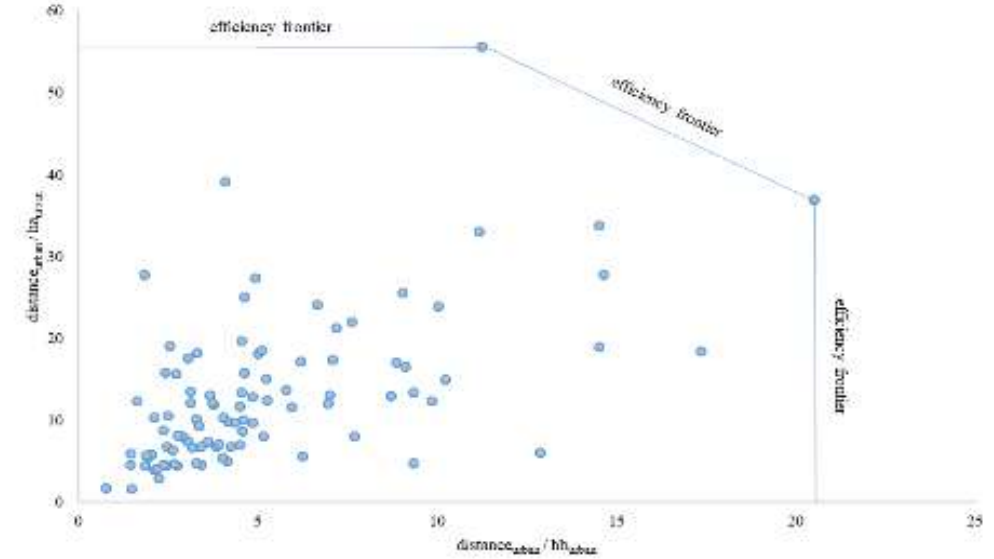
Road types:

- Urban road network (signalized or not network, speed limit ≤ 50 km/h)
- Urban express road network (speed limit 50 – 90 km/h)
- Highways (speed limit ≥ 90 km/h)



Driving efficiency analysis using DEA

- DEA results **2-D illustration**
 - Urban
 - Rural
- DEA **inputs**
 - Number of harsh acceleration events
 - Number of harsh braking events
- DEA **outputs**
 - Trip distance



Data preparation

- Data are **anonymized**
 - user-agnostic approach
 - identify driving behaviors and patterns
 - causality between behaviour and other factors
 - large-scale samples
 - no information on demographics or accident record
- **Python** programming language
 - filter aggregate data
 - retain only necessary information
 - aggregate data
 - data analysis



Trip efficiency analysis (1/3)

- **Convex Hull** technique outperforms
- Significant **time reduction**
 - As the database becomes larger
 - Convex Hull DEA – 5 minutes
 - RBE DEA – 12.6 days
 - Standard DEA – 40.7 days

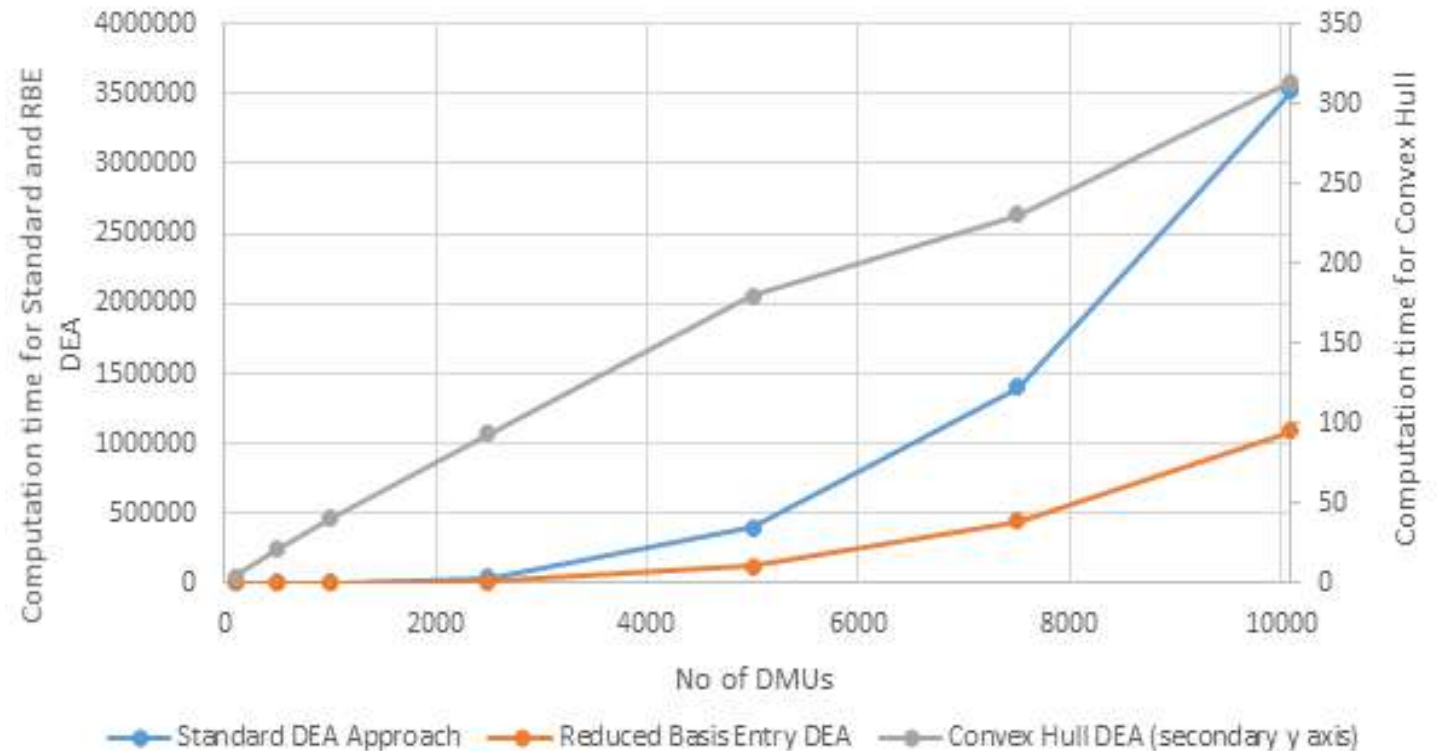
No of DMUs	Computation time (sec)			CH DEA % computation time improvement over		RBE DEA % computation time improvement over Standard DEA
	Standard DEA Approach	RBE DEA	Convex Hull DEA	Standard DEA Approach	RBE DEA	
100	11	6	4	63.64%	33.33%	45.45%
500	477	169	21	95.60%	87.57%	64.57%
1000	3250	1121	41	98.74%	96.34%	65.51%
2500	44435	15570	94	99.79%	99.40%	64.96%
5000	398485	123986	180	99.95%	99.85%	68.89%
7500	1400909	444498	231	99.98%	99.95%	68.27%
10088	3519372	1089731	314	99.99%	99.97%	69.04%

* Inputs = [ha_{urban}, ha_{rural}, ha_{highway}], Outputs = [distance_{urban}, distance_{rural}, distance_{highway}]



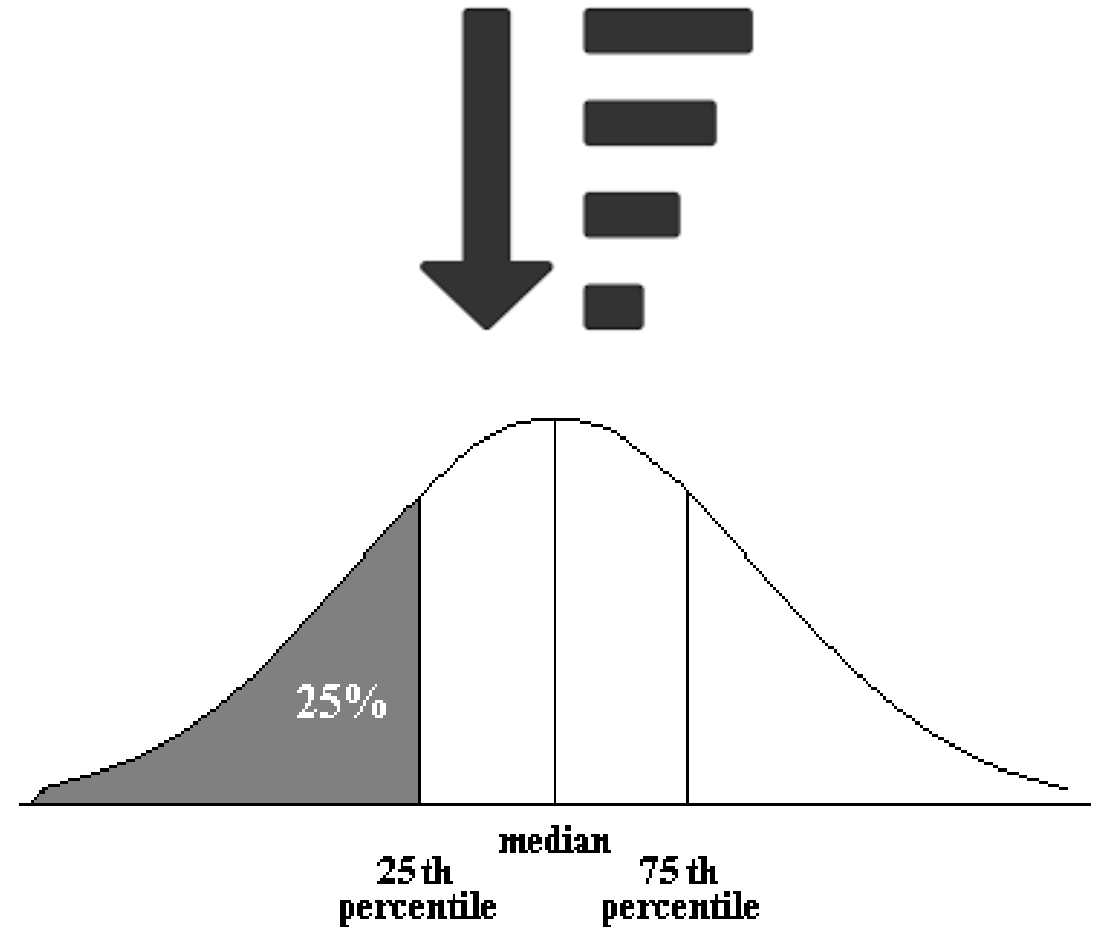
Trip efficiency analysis (2/3)

- **Convex Hull** DEA
 - linearly increased
- **Standard** and **RBE** DEA
 - Exponentially increased



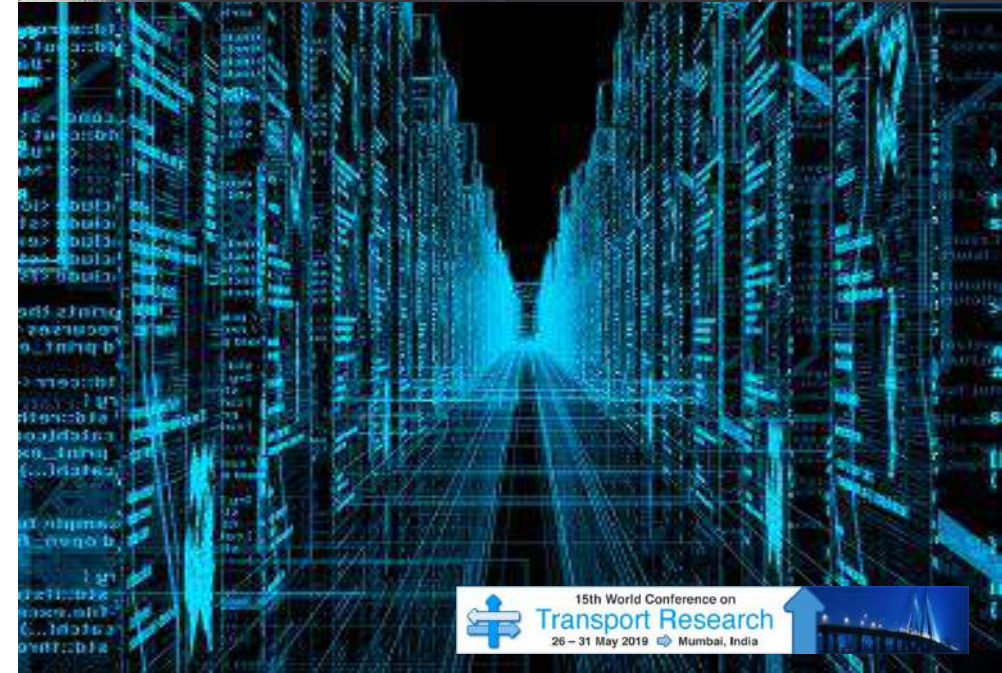
Trip efficiency analysis (3/3)

- **Least efficient** trips
- **Efficiency** estimation
- **Sort**
 - larger to smaller
- **Percentile**
 - 5%, 10%, 25% etc.



Conclusions

- **Innovative** methodological approach for driving efficiency benchmarking as well as for estimating the efficient level of metrics for each trip.
- The integration of DEA with the convex hull algorithmic approach yielded **significantly better** results than the rest of the approaches tested.



Future research

- Exploit a **larger** driving **sample**
- Overcome **DEA limitations** – zero sum input attributes
- Increase the number of **attributes**
 - headways
 - lane changing
 - eye movement
 - drowsiness





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